Display 1 A: Average Percent Correct on 1995 TIMSS Mathematics Items

| Grade 3 |  |
| :--- | :---: |
| Nation | Average |
| Korea | 67 |
| Japan | 63 |
| Singapore | 62 |
| District A | 62 |
| Hong Kong | 59 |
| Czech Republic | 52 |
| Netherlands | 52 |
| Slovenia | 51 |
| Australia | 50 |
| Austria | 50 |
| Hungary | 49 |
| United States | 49 |
| Ireland | 48 |
| Canada | 47 |
| International Mean | 47 |
| Latvia (LSS) | 45 |
| Scotland | 45 |
| England | 45 |
| New Zealand | 41 |
| Thailand | 40 |
| Cyprus | 38 |
| Greece | 37 |
| Portugal | 37 |
| Norway | 36 |
| Iceland | 35 |
| Iran, Islamic Republic | 28 |


| Grade 4 |  |
| :--- | :---: |
| Nation | Average |
| Korea | 76 |
| Singapore | 76 |
| Japan | 74 |
| Hong Kong | 73 |
| District A | 72 |
| Netherlands | 69 |
| Czech Republic | 66 |
| Austria | 65 |
| Hungary | 64 |
| Slovenia | 64 |
| Australia | 63 |
| Ireland | 63 |
| United States | 63 |
| Canada | 60 |
| Israel | 59 |
| International Mean | 59 |
| Latvia (LSS) | 59 |
| Scotland | 58 |
| England | 57 |
| Cyprus | 54 |
| Norway | 53 |
| New Zealand | 53 |
| Greece | 51 |
| Thailand | 50 |
| Iceland | 50 |
| Portugal | 48 |
| Iran, Islamic Republic | 38 |
| Kuwait | 32 |
|  |  |


| Grade 7 |  |
| :---: | :---: |
| Nation | Average |
| Singapore | 73 |
| Japan | 67 |
| Korea | 67 |
| Hong Kong | 65 |
| Belgium (FI) | 65 |
| District A | 60 |
| Czech Republic | 57 |
| Austria | 56 |
| Netherlands | 55 |
| Bulgaria | 55 |
| Slovak Republic | 54 |
| Hungary | 54 |
| Belgium (Fr) | 54 |
| Switzerland | 53 |
| Slovenia | 53 |
| Russian Federation | 53 |
| Ireland | 53 |
| Australia | 52 |
| Canada | 52 |
| Thailand | 52 |
| France | 51 |
| International Mean | 49 |
| Germany | 49 |
| United States | 48 |
| Sweden | 47 |
| England | 47 |
| New Zealand | 46 |
| Norway | 44 |
| Denmark | 44 |
| Scotland | 44 |
| Latvia (LSS) | 44 |
| Iceland | 43 |
| Romania | 43 |
| Spain | 42 |
| Cyprus | 42 |
| Greece | 40 |
| Lithuania | 38 |
| Portugal | 37 |
| Iran, Islamic Republic | 32 |
| Colombia | 26 |
| South Africa | 23 |


| Grade 8 |  |
| :---: | :---: |
| Nation | Average |
| Singapore | 79 |
| Japan | 73 |
| Korea | 72 |
| Hong Kong | 70 |
| Belgium (FI) | 66 |
| Czech Republic | 66 |
| District A | 64 |
| Slovak Republic | 62 |
| Switzerland | 62 |
| Austria | 62 |
| Hungary | 62 |
| Slovenia | 61 |
| France | 61 |
| Netherlands | 60 |
| Bulgaria | 60 |
| Russian Federation | 60 |
| Ireland | 59 |
| Canada | 59 |
| Belgium (Fr) | 59 |
| Australia | 58 |
| Sweden | 56 |
| Israel | 57 |
| Thailand | 57 |
| International Mean | 55 |
| Germany | 54 |
| New Zealand | 54 |
| Norway | 54 |
| England | 53 |
| United States | 53 |
| Denmark | 52 |
| Scotland | 52 |
| Latvia (LSS) | 51 |
| Spain | 51 |
| Iceland | 50 |
| Greece | 49 |
| Romania | 49 |
| Lithuania | 48 |
| Cyprus | 48 |
| Portugal | 43 |
| Iran, Islamic Republic | 38 |
| Kuwait | 30 |
| Colombia | 29 |
| South Africa | 24 |

Display 1B: Average Percent Correct on 1995 TIMSS Mathematics Items

| Grade 3 |  |
| :--- | :---: |
| Nation | Average |
| Korea | 67 |
| Japan | 63 |
| Singapore | 62 |
| Hong Kong | 59 |
| Czech Republic | 52 |
| Netherlands | 52 |
| District B | 52 |
| Slovenia | 51 |
| Australia | 50 |
| Austria | 50 |
| Hungary | 49 |
| United States | 49 |
| Ireland | 48 |
| Canada | 47 |
| International Mean | 47 |
| Latvia (LSS) | 45 |
| Scotland | 45 |
| England | 45 |
| New Zealand | 41 |
| Thailand | 40 |
| Cyprus | 38 |
| Greece | 37 |
| Portugal | 37 |
| Norway | 36 |
| Iceland | 35 |
| Iran, Islamic Republic | 28 |


| Grade 4 |  |
| :--- | :---: |
| Nation | Average |
| Korea | 76 |
| Singapore | 76 |
| Japan | 74 |
| Hong Kong | 73 |
| Netherlands | 69 |
| Czech Republic | 66 |
| Austria | 65 |
| Hungary | 64 |
| Slovenia | 64 |
| District B | 64 |
| Australia | 63 |
| Ireland | 63 |
| United States | 63 |
| Canada | 60 |
| Israel | 59 |
| International Mean | 59 |
| Latvia (LSS) | 59 |
| Scotland | 58 |
| England | 57 |
| Cyprus | 54 |
| Norway | 53 |
| New Zealand | 53 |
| Greece | 51 |
| Thailand | 50 |
| Iceland | 50 |
| Portugal | 48 |
| Iran, Islamic Republic | 38 |
| Kuwait | 32 |


| Grade 7 |  |
| :---: | :---: |
| Nation | Average |
| Singapore | 73 |
| Japan | 67 |
| Korea | 67 |
| Hong Kong | 65 |
| Belgium (FI) | 65 |
| Czech Republic | 57 |
| Austria | 56 |
| Netherlands | 55 |
| Bulgaria | 55 |
| Slovak Republic | 54 |
| Hungary | 54 |
| Belgium (Fr) | 54 |
| Switzerland | 53 |
| Slovenia | 53 |
| Russian Federation | 53 |
| Ireland | 53 |
| Australia | 52 |
| Canada | 52 |
| Thailand | 52 |
| France | 51 |
| District B | 50 |
| International Mean | 49 |
| Germany | 49 |
| United States | 48 |
| Sweden | 47 |
| England | 47 |
| New Zealand | 46 |
| Norway | 44 |
| Denmark | 44 |
| Scotland | 44 |
| Latvia (LSS) | 44 |
| Iceland | 43 |
| Romania | 43 |
| Spain | 42 |
| Cyprus | 42 |
| Greece | 40 |
| Lithuania | 38 |
| Portugal | 37 |
| Iran, Islamic Republic | 32 |
| Colombia | 26 |
| South Africa | 23 |


| Grade 8 |  |
| :--- | :---: |
| Ningapore | Average |
| Japan | 79 |
| Korea | 73 |
| Hong Kong | 72 |
| Belgium (FI) | 70 |
| Czech Republic | 66 |
| Slovak Republic | 66 |
| Switzerland | 62 |
| Austria | 62 |
| Hungary | 62 |
| Slovenia | 62 |
| France | 61 |
| Netherlands | 61 |
| Bulgaria | 60 |
| Russian Federation | 60 |
| Ireland | 60 |
| Canada | 59 |
| Belgium (Fr) | 59 |
| Australia | 59 |
| Sweden | 58 |
| Israel | 56 |
| Thailand | 57 |
| International Mean | 57 |
| District B | 55 |
| Germany | 55 |
| New Zealand | 54 |
| Norway | 54 |
| England | 54 |
| United States | 53 |
| Denmark | 53 |
| Scotland | 52 |
| Latvia (LSS) | 52 |
| Spain | 51 |
| Iceland | 51 |
| Greece | 50 |
| Romania | 49 |
| Lithuania | 49 |
| Cyprus | 48 |
| Portugal | 48 |
| Iran, Islamic Republic | 43 |
| Kuwait | 38 |
| Colombia | 30 |
| South Africa | 29 |
|  | 24 |
|  |  |

Display 2A: Average Percent Correct on TIMSS 1995 End-of-Secondary Mathematics Literacy Test

| Nation | Average |
| :--- | :---: |
| Netherlands | 68 |
| Sweden | 64 |
| Denmark | 64 |
| Iceland | 62 |
| Switzerland | 62 |
| New Zealand | 61 |
| Norway | 60 |
| Australia | 60 |
| France | 60 |
| District A - Grade 9 | 60 |
| Canada | 58 |
| Austria | 58 |
| Slovenia | 58 |
| Germany | 53 |
| International Mean | 50 |
| Italy | 50 |
| Russian Federation | 49 |
| Lithuania | 48 |
| United States - Grade 12 | 46 |
| Hungary | 46 |
| Israel | 45 |
| Czech Republic | 45 |
| Cyprus | 40 |
| South Africa | 25 |


| Nation | Average |
| :--- | :---: |
| Netherlands | 68 |
| Sweden | 64 |
| Denmark | 64 |
| Iceland | 62 |
| Switzerland | 62 |
| District A Grade 10 | 61 |
| New Zealand | 61 |
| Norway | 60 |
| Australia | 60 |
| France | 60 |
| Canada | 58 |
| Austria | 58 |
| Slovenia | 58 |
| Germany | 53 |
| International Mean | 50 |
| Italy | 50 |
| Russian Federation | 49 |
| Lithuania | 48 |
| United States - Grade 12 | 46 |
| Hungary | 46 |
| Israel | 45 |
| Czech Republic | 45 |
| Cyprus | 40 |
| South Africa | 25 |


| Nation | Average |
| :--- | :---: |
| Netherlands | 68 |
| Sweden | 64 |
| Denmark | 64 |
| District A - Grade 11 | 62 |
| Iceland | 62 |
| Switzerland | 62 |
| New Zealand | 61 |
| Norway | 60 |
| Australia | 60 |
| France | 60 |
| Canada | 58 |
| Austria | 58 |
| Slovenia | 58 |
| Germany | 53 |
| International Mean | 50 |
| Italy | 50 |
| Russian Federation | 49 |
| Lithuania | 48 |
| United States - Grade 12 | 46 |
| Hungary | 46 |
| Israel | 45 |
| Czech Republic | 45 |
| Cyprus | 40 |
| South Africa | 25 |


| Nation | Average |
| :--- | :---: |
| Netherlands | 68 |
| Sweden | 64 |
| Denmark | 64 |
| District A Grade 12 | 62 |
| Iceland | 62 |
| Switzerland | 62 |
| New Zealand | 61 |
| Norway | 60 |
| Australia | 60 |
| France | 60 |
| Canada | 58 |
| Austria | 58 |
| Slovenia | 58 |
| Germany | 53 |
| International Mean | 50 |
| Italy | 50 |
| Russian Federation | 49 |
| Lithuania | 48 |
| United States - Grade 12 | 46 |
| Hungary | 46 |
| Israel | 45 |
| Czech Republic | 45 |
| Cyprus | 40 |
| South Africa | 25 |

[^0]Display 2B: Average Percent Correct on TIMSS 1995 End-of-Secondary Mathematics Literacy Test

| Nation | Average | Nation | Average |
| :---: | :---: | :---: | :---: |
| Netherlands | 68 | Netherlands | 68 |
| Sweden | 64 | Sweden | 64 |
| Denmark | 64 | Denmark | 64 |
| Iceland | 62 | Iceland | 62 |
| Switzerland | 62 | Switzerland | 62 |
| New Zealand | 61 | New Zealand | 61 |
| Norway | 60 | Norway | 60 |
| Australia | 60 | Australia | 60 |
| France | 60 | France | 60 |
| Canada | 58 | Canada | 58 |
| Austria | 58 | Austria | 58 |
| Slovenia | 58 | Slovenia | 58 |
| Germany | 53 | Germany | 53 |
| International Mean | 50 | International Mean | 50 |
| Italy | 50 | Italy | 50 |
| Russian Federation | 49 | Russian Federation | 49 |
| Lithuania | 48 | Lithuania | 48 |
| United States - Grade 12 | 46 | United States - Grade 12 | 46 |
| Hungary | 46 | Hungary | 46 |
| Israel | 45 | Israel | 45 |
| Czech Republic | 45 | Czech Republic | 45 |
| District B - Grade 9 | 40 | District B - Grade 10 | 42 |
| Cyprus | 40 | Cyprus | 40 |
| South Africa | 25 | South Africa | 25 |


| Nation | Average |
| :--- | :---: |
| Netherlands | 68 |
| Sweden | 64 |
| Denmark | 64 |
| Iceland | 62 |
| Switzerland | 62 |
| New Zealand | 61 |
| Norway | 60 |
| Australia | 60 |
| France | 60 |
| Canada | 58 |
| Austria | 58 |
| Slovenia | 58 |
| Germany | 53 |
| International Mean | 50 |
| Italy | 50 |
| Russian Federation | 49 |
| Lithuania | 48 |
| United States - Grade 12 | 46 |
| Hungary | 46 |
| Israel | 45 |
| Czech Republic | 45 |
| District B - Grade 11 | 44 |
| Cyprus | 40 |
| South Africa | 25 |


| Nation | Average |
| :--- | :---: |
| Netherlands | 68 |
| Sweden | 64 |
| Denmark | 64 |
| Iceland | 62 |
| Switzerland | 62 |
| New Zealand | 61 |
| Norway | 60 |
| Australia | 60 |
| France | 60 |
| Canada | 58 |
| Austria | 58 |
| Slovenia | 58 |
| Germany | 53 |
| International Mean | 50 |
| Italy | 50 |
| Russian Federation | 49 |
| Lithuania | 48 |
| United States - Grade 12 | 46 |
| Hungary | 46 |
| Israel | 45 |
| Czech Republic | 45 |
| District B - Grade 12 | 44 |
| Cyprus | 40 |
| South Africa | 25 |

[^1]Display 3: Average \% Correct on 1995 TIMSS 8th Grade Mathematics Items at Each Grade


Display 4: Number of PROM/SE Districts in Relation to the 1995 TIMSS US Mean Mathematics Performance


Display 5: Boxplots of Average Percent Correct Across all PROM/SE Mathematics Items for All PROM/SE Districts at Each Grade


Display 6: Boxplots of Average Percent Correct Across all PROM/SE Mathematics Items for All PROM/SE Schools at Each Grade


Display 7: Boxplots of Average Percent Correct on Select PROM/SE Elementary Mathematics Strands for All PROM/SE Schools at Each Grade


Display 8: Boxplots of Average Percent Correct on Select PROM/SE Middle School Mathematics Strands for All PROM/SE Schools at Each Grade


Display 9: Boxplots of Average Percent Correct on Select PROM/SE High School Mathematics Strands for All PROM/SE Schools at Each Grade


## Display 10: Number of Mathematics Topics Intended at Each Grade

- Gray bars show how many mathematics topics were intended to be covered at each grade in the 1995 TIMSS countries.
- The bars extend from the 25 th percentile to the 75 th percentile.
- The black line indicates the median number of topics at each grade.


Display 11: Mathematics Topics Intended at Each Grade by Top-Achieving Countries

|  | Grade |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Topic | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Whole Number: Meaning |  |  |  | $\bigcirc$ | - |  |  |  |
| Whole Number: Operations | $\square$ |  | - | - | - |  |  |  |
| Measurement Units | - | - | - | $\square$ | $\square$ | $\square$ | $\bigcirc$ |  |
| Common Fractions |  |  | $\triangle$ | $\square$ | $\square$ | - |  |  |
| Equations \& Formulas |  |  | - | - | - | - | $\square$ |  |
| Data Representation \& Analysis |  |  | $\Delta$ | $\Delta$ | $\bigcirc$ | - |  | - |
| 2-D Geometry: Basics |  |  | A | - | $\bigcirc$ | - | $\square$ | $\square$ |
| 2-D Geometry: Polygons \& Circles |  |  |  | - | - | - | $\square$ | $\square$ |
| Measurement: Perimeter, Area \& Volume |  |  |  | - | - | - | - | $\Delta$ |
| Rounding \& Significant Figures |  |  |  | $\bigcirc$ | $\bigcirc$ |  |  |  |
| Estimating Computations |  |  |  | $\bigcirc$ | - | - |  |  |
| Whole Numbers: Properties of Operations |  |  |  | $\triangle$ | - |  |  |  |
| Estimating Quantity \& Size |  |  |  | $\triangle$ | $\triangle$ |  |  |  |
| Decimal Fractions |  |  |  | $\bigcirc$ | $\square$ | - |  |  |
| Relation of Common \& Decimal Fractions |  |  |  | $\bigcirc$ | $\square$ | - |  |  |
| Properties of Common \& Decimal Fractions |  |  |  |  | - | - |  |  |
| Percentages |  |  |  |  | $\bigcirc$ | - |  |  |
| Proportionality Concepts |  |  |  |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\Delta$ |
| Proportionality Problems |  |  |  |  | - | $\bigcirc$ | $\square$ | $\square$ |
| 2-D Geometry: Coordinate Geometry |  |  |  |  | $\triangle$ | - | - | - |
| Geometry: Transformations |  |  |  |  |  | $\bigcirc$ | - | - |
| Negative Numbers, Integers, \& Their Properties |  |  |  |  |  | A | - |  |
| Number Theory |  |  |  |  |  |  | $\bullet$ | $\Delta$ |
| Exponents, Roots \& Radicals |  |  |  |  |  |  | - | $\bigcirc$ |
| Exponents \& Orders of Magnitude |  |  |  |  |  |  | $\Delta$ | A |
| Measurement: Estimation \& Errors |  |  |  |  |  |  | - |  |
| Constructions Using Straightedge \& Compass |  |  |  |  |  |  |  | $\Delta$ |
| 3-D Geometry |  |  |  |  |  |  | - | - |
| Geometry: Congruence \& Similarity |  |  |  |  |  |  |  | $\square$ |
| Rational Numbers \& Their Properties |  |  |  |  |  |  |  | $\Delta$ |
| Patterns, Relations \& Functions |  |  |  |  |  |  |  | - |
| Proportionality: Slope \& Trigonometry |  |  |  |  |  |  |  | $\underline{1}$ |
| \# of additional topics covered at grade level, on average | $\underline{2}$ | $\underline{6}$ | 5 | $\underline{1}$ | $\underline{1}$ | $\underline{3}$ | $\underline{6}$ | $\underline{3}$ |
| \# of possible topics from which additional topics may be selected | 4 | 7 | 8 | 1 | 2 | 5 | 10 | 7 |
| Intended by 4 out of the 6 to | -ac | ing | tries | - |  |  |  |  |
| Intended by all but one of the top-achieving co | untr | 5 |  | - |  |  |  |  |
| Intended by all of the top | -ach |  |  |  |  |  |  |  |

Display 12A: Mathematics Topics Intended at Each Grade in District A's State Content Standards

|  | Grade |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Topic | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Whole Number: Meaning | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |  |
| Whole Number: Operations | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |  |  |  |  |
| Measurement Units | $\bigcirc$ | - | $\bigcirc$ | - | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Common Fractions |  |  |  |  | - | $\bigcirc$ | $\bigcirc$ |  |
| Equations \& Formulas | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Data Representation \& Analysis | - | - | $\bigcirc$ | - | - | $\bigcirc$ | $\bigcirc$ | - |
| 2-D Geometry: Basics | $\bigcirc$ | - | $\bigcirc$ | - | - | - | $\bigcirc$ |  |
| 2-D Geometry: Polygons \& Circles | - | - | $\bigcirc$ | $\bigcirc$ | - | - | $\bigcirc$ | $\bigcirc$ |
| Measurement: Perimeter, Area \& Volume |  |  |  |  | - | - | $\bigcirc$ | $\bigcirc$ |
| Rounding \& Significant Figures | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Estimating Computations | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | - |
| Whole Numbers: Properties of Operations | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |  |  |  |  |
| Estimating Quantity \& Size | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Decimal Fractions | - | - | - | $\bigcirc$ | - | $\bigcirc$ | - |  |
| Relation of Common \& Decimal Fractions | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |  |
| Properties of Common \& Decimal Fractions |  |  |  |  | - | - | $\bigcirc$ |  |
| Percentages |  |  |  |  | $\bigcirc$ | - | $\bigcirc$ |  |
| Proportionality Concepts |  |  |  |  | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Proportionality Problems |  |  |  |  |  |  |  |  |
| 2-D Geometry: Coordinate Geometry | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | - | - | - | - |
| Geometry: Transformations | - | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |  | - |
| Negative Numbers, Integers, \& Their Properties |  |  |  |  |  |  |  |  |
| Number Theory |  |  |  |  | - | $\bigcirc$ | - | $\bigcirc$ |
| Exponents, Roots \& Radicals |  |  |  |  |  |  |  | - |
| Exponents \& Orders of Magnitude |  |  |  |  |  |  |  |  |
| Measurement: Estimation \& Errors | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Constructions Using Straightedge \& Compass | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| 3-D Geometry | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | - | - | - | - |
| Geometry: Congruence \& Similarity |  | $\bigcirc$ |  | - | - | $\bigcirc$ | - | $\bigcirc$ |
| Rational Numbers \& Their Properties |  |  |  |  | - | - | $\bigcirc$ |  |
| Patterns, Relations \& Functions | - | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ |
| Proportionality: Slope \& Trigonometry |  |  |  |  |  |  |  |  |
| Number of additional topics intended | 2 | 2 | 2 | 2 | 2 | 2 | 2 | 3 |
| Intended in the State's Content Stand Top-achieving countries' intended-topics p |  | $\bullet$ |  |  |  |  |  |  |

Display 12B: Mathematics Topics Intended at Each Grade in District B's State Content Standards

|  | Grade |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Topic | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Whole Number: Meaning | $\bigcirc$ | $\bigcirc$ | - | - | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Whole Number: Operations | - | - | - | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Measurement Units | - | - | $\bigcirc$ | - | - | $\bullet$ | - | $\bullet$ |
| Common Fractions | - | - | - | - | - | - | $\bigcirc$ | - |
| Equations \& Formulas | $\bullet$ | - | - | $\bigcirc$ | - | $\bullet$ | - | $\bullet$ |
| Data Representation \& Analysis | - | - | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| 2-D Geometry: Basics | $\bullet$ | - | - | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ |
| 2-D Geometry: Polygons \& Circles | - | - | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ |
| Measurement: Perimeter, Area \& Volume | - | - | - | - | - | - | - | - |
| Rounding \& Significant Figures | - | - | $\bullet$ | - | - | $\bullet$ | $\bullet$ | $\bullet$ |
| Estimating Computations | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Whole Numbers: Properties of Operations | $\bullet$ | - | $\bullet$ | - |  |  |  |  |
| Estimating Quantity \& Size | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Decimal Fractions | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ |
| Relation of Common \& Decimal Fractions | $\bullet$ | - | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Properties of Common \& Decimal Fractions | - | - | $\bullet$ | - | - | - | $\bullet$ | $\bullet$ |
| Percentages |  |  |  |  | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Proportionality Concepts | $\bullet$ | - | - | $\bullet$ | - | $\bullet$ | - | - |
| Proportionality Problems | - | $\bullet$ | $\bullet$ | - | - | $\bullet$ | - | $\bullet$ |
| 2-D Geometry: Coordinate Geometry | - | $\bullet$ | $\bullet$ | - | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ |
| Geometry: Transformations | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | - |
| Negative Numbers, Integers, \& Their Properties | - | $\bullet$ | - | - | $\bullet$ | - | - | $\bullet$ |
| Number Theory | $\bullet$ | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Exponents, Roots \& Radicals | - | $\bullet$ | $\bullet$ | - | $\bullet$ | $\bullet$ | - | - |
| Exponents \& Orders of Magnitude | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Measurement: Estimation \& Errors | - | $\bullet$ | $\bullet$ | - | $\bullet$ | $\bullet$ | - | $\bullet$ |
| Constructions using Straightedge \& Compass | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| 3-D Geometry | - | $\bullet$ | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Geometry: Congruence \& Similarity | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Rational Numbers \& Their Properties | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Patterns, Relations \& Functions | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Proportionality: Slope \& Trigonometry | - | - | - | - | - | - | $\bigcirc$ | $\bigcirc$ |
| Number of additional topics intended | 9 | 9 | 9 | 9 | 10 | 10 | 10 | 10 |
| Intended in the State's Content Stand Top-achieving countries' intended-topics |  | $\bullet$ |  |  |  |  |  |  |

Display 13A: Mathematics Topics Intended at Each Grade by District A

|  | Grade |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Topic | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Whole Number: Meaning | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |  |  |  |
| Whole Number: Operations | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Measurement Units |  | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Common Fractions |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |  |
| Equations \& Formulas |  |  |  |  |  |  | $\bigcirc$ | $\bigcirc$ |
| Data Representation \& Analysis | - | - | $\bigcirc$ | - | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| 2-D Geometry: Basics |  |  |  |  |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| 2-D Geometry: Polygons \& Circles |  |  |  |  | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| Measurement: Perimeter, Area \& Volume |  | $\bigcirc$ | $\bigcirc$ |  | $\bigcirc$ |  |  |  |
| Rounding \& Significant Figures |  |  |  |  |  |  |  |  |
| Estimating Computations |  | - | - | $\bigcirc$ | - | $\bigcirc$ | - | $\bigcirc$ |
| Whole Numbers: Properties of Operations |  |  |  |  |  |  |  | $\bigcirc$ |
| Estimating Quantity \& Size |  |  |  |  |  |  |  |  |
| Decimal Fractions |  |  |  | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |  |
| Relation of Common \& Decimal Fractions |  |  |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Properties of Common \& Decimal Fractions |  |  |  |  |  |  |  | $\bigcirc$ |
| Percentages |  |  |  |  |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Proportionality Concepts |  |  |  |  |  |  | $\bigcirc$ |  |
| Proportionality Problems |  |  |  |  |  |  | $\bigcirc$ | $\bigcirc$ |
| 2-D Geometry: Coordinate Geometry |  |  | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Geometry: Transformations |  | - |  |  |  | $\bigcirc$ | $\bigcirc$ | - |
| Negative Numbers, Integers, \& Their Properties |  |  | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Number Theory |  |  |  | - | - | $\bigcirc$ | $\bigcirc$ |  |
| Exponents, Roots \& Radicals |  |  |  |  |  | - | - | - |
| Exponents \& Orders of Magnitude |  |  |  |  |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Measurement: Estimation \& Errors |  |  |  |  |  |  |  |  |
| Constructions Using Straightedge \& Compass |  |  |  |  |  |  |  |  |
| 3-D Geometry |  |  |  |  | $\bigcirc$ |  | $\bigcirc$ | $\bigcirc$ |
| Geometry: Congruence \& Similarity |  |  |  |  |  | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Rational Numbers \& Their Properties |  |  |  |  |  |  |  |  |
| Patterns, Relations \& Functions | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Proportionality: Slope \& Trigonometry |  |  |  |  | $\bigcirc$ | , | $\bigcirc$ | $\bigcirc$ |
| Intended in District A's Content Stan Top-achieving countries' intended-topics |  | $\bigcirc$ |  |  |  |  |  |  |

Display 13B: Mathematics Topics Intended at Each Grade by District B

|  | Grade |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Topic | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Whole Number: Meaning | - | - | $\bigcirc$ | - | $\bigcirc$ |  |  |  |
| Whole Number: Operations | $\bigcirc$ | - | - | - | - | $\bullet$ |  |  |
| Measurement Units | - | - | $\bigcirc$ | - | $\bullet$ | $\bigcirc$ | - | - |
| Common Fractions | $\bullet$ | - | - | - | - | $\bigcirc$ | $\bigcirc$ | $\bigcirc$ |
| Equations \& Formulas | $\bullet$ | - | - | - | - | $\bullet$ | - | $\bullet$ |
| Data Representation \& Analysis | $\bullet$ | - | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ | $\bullet$ |
| 2-D Geometry: Basics |  |  |  | $\bullet$ | $\bigcirc$ | - | $\bigcirc$ | $\bigcirc$ |
| 2-D Geometry: Polygons \& Circles | - |  | - | - | - | - | - | - |
| Measurement: Perimeter, Area \& Volume |  |  |  | $\bullet$ | $\bigcirc$ | - | - | $\bigcirc$ |
| Rounding \& Significant Figures |  |  | - | - | - | $\bullet$ | $\bullet$ | $\bullet$ |
| Estimating Computations |  | - | $\bullet$ | $\bigcirc$ | - | - | $\bullet$ | $\bullet$ |
| Whole Numbers: Properties of Operations |  | - | $\bigcirc$ | - | $\bigcirc$ |  | $\bullet$ | $\bullet$ |
| Estimating Quantity \& Size | $\bullet$ | - | $\bullet$ | - | - |  | $\bullet$ |  |
| Decimal Fractions |  |  |  | - | - | $\bullet$ | $\bullet$ | $\bullet$ |
| Relation of Common \& Decimal Fractions |  |  |  | - | $\bullet$ | - | $\bullet$ | $\bigcirc$ |
| Properties of Common \& Decimal Fractions |  |  |  |  | $\bigcirc$ | $\bigcirc$ | - | $\bullet$ |
| Percentages |  |  |  |  | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Proportionality Concepts |  |  |  |  |  | $\bullet$ | - | $\bullet$ |
| Proportionality Problems |  |  |  |  |  | $\bullet$ | $\bullet$ | $\bigcirc$ |
| 2-D Geometry: Coordinate Geometry |  |  | $\bullet$ |  | - | - | - | - |
| Geometry: Transformations |  | - | $\bullet$ | - | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ |
| Negative Numbers, Integers, \& Their Properties |  |  |  |  |  | $\bullet$ | - | $\bullet$ |
| Number Theory |  |  |  |  | $\bullet$ | $\bullet$ | $\bullet$ | $\bigcirc$ |
| Exponents, Roots \& Radicals |  |  |  |  |  |  | - | - |
| Exponents \& Orders of Magnitude |  |  |  |  |  | - | - | - |
| Measurement: Estimation \& Errors |  |  | - | $\bullet$ | $\bigcirc$ | $\bullet$ | $\bullet$ | $\bullet$ |
| Constructions using Straightedge \& Compass |  |  |  |  | - |  | $\bigcirc$ | $\bullet$ |
| 3-D Geometry |  |  |  |  |  | - | - | $\bigcirc$ |
| Geometry: Congruence \& Similarity |  |  | - | - | $\bullet$ | $\bullet$ |  | $\bullet$ |
| Rational Numbers \& Their Properties |  |  |  |  |  | $\bullet$ | $\bullet$ | $\bullet$ |
| Patterns, Relation \& Functions |  | - | - |  |  | $\bullet$ | $\bullet$ | $\bullet$ |
| Proportionality: Slope \& Trigonometry |  |  |  |  |  |  |  |  |

Intended in District B's Content Standards
Top-achieving countries' intended-topics profile

Display 14A: Percent Teaching Time in Nine Broad Mathematics Areas at Each Grade in District A


Display 14B: Percent Teaching Time in Nine Broad Mathematics Areas at Each Grade in District B


Display 16A: Percent Teaching Time in Nine Broad Mathematics Areas at 7th and 8th Grade for the USA, Top-Achieving Countries, and District A


Display 16B: Percent Teaching Time in Nine Broad Mathematics Areas at 7th and 8th Grade for the USA, Top-Achieving Countries, and District B


Display 17: Boxplots of Percent Teaching Time for Whole Numbers Across Teachers at Each Grade for District A


Display 18: Boxplots of Percent Teaching Time for Common Fractions Across Teachers at Each Grade for District A


Display 19: Boxplots of Percent Teaching Time for Number (Basic) Across Teachers at Each Grade for District A


Display 20: Boxplots of Percent Teaching Time for Geometric Relationships Across Teachers at Each Grade for District A


# Displays 14-16: Elementary Mathematics Areas Key 


) Whole number meaning - place value \& numeration; ordering \& comparing; operations \& properties of operations
Operations \& Properties - addition, subtraction, multiplication, division, mixed operations; associative, commutative, identity, distributive, \& other properties
3) Common Fractions - meaning, representation, uses, computations; computations with mixed numbers
Number 4) Decimal Fractions - meaning, representation, uses, computations (Transition)
5) Relationships Between Common \& Decimal Fractions - equivalence, conversions \& ordering
6) Percentages - concepts, problems, \& computations
7) Properties of Common \& Decimal Fractions - commutative, distributive, identity, inverse, etc.

| Algebra | 8)Number Sets \& Concepts - integers (negative \& positive); rational, realy, <br> and other number sets |
| :---: | :--- |
| Foundations | 9)Other Number Topics - binary arithmetic; bases other than ten; exponents, <br> roots. \& radicals: complex numbers |
|  | 10) <br> svstematic countina |
| Number <br> (Basic) | 11) <br> Estimation \& Number Sense - estimating quantity \& size; rounding, <br> significant figures, \& estimating computations (and deciding if solutions are <br> reasonable: scientific notation |

Measurement

| Measurement | 12) | Units \& Processes - ideas of measurement and units; standard nonstandard units (e.g., inches, liters, paper clips); common measures of length, area, time, temperature, money, mass, etc.; miles/hour, miles/gal., etc.; use of measurement instruments |
| :---: | :---: | :---: |
| Geometric Relationships | 13) | Perimeter, Area, \& Volume - computations, formulas, \& properties (including surface area) |
| Measurement | 14) | Estimation \& Measurement Errors - precision, accuracy, \& errors of measurement |
| Geometry |  |  |
| Geometric Objects | 15) | Basics - number lines, coordinate system; graphs in two dimensions; lines, segments, rays; angles; equations of straight lines; parallelism \& perpendicularitv |

Geometric 16) Two Dimensional Figures - classification \& properties of polygons \& circles;
Relationships Pythagorean theorem
17) Three Dimensional Geomery - 3-D coordinate systems, spatial visualization; shapes \& surfaces, planes, vectors; constructions with straiahtedqe \& compass
Geometric
Objects
18) Transformations - patterns, tessellations, friezes; symmetry, rotation, \& reflections
Geometric Relationships 19) Congruence \& Similarity - properties of congruence \& similarity Proportionality, Functions \& Equations

| Number <br> (Transition) |  | Proportionality Concepts - meaning of ratio \& proportion; direct \& inverse proportion <br> Proportionality Problems - scales, maps, models, proportional equations |
| :---: | :---: | :---: |
| Intermediate Algebra | 22 | Slope \& Trigonometry - slope \& interpolation; sines \& cosines |
| Beginning | 23) | Patterns, Relations, \& Functions - number patterns, relations, properties, uses, \& graphs of functions; types of functions, relations of functions and equations |
| Algebra |  | Linear Equations \& Formulas - representing linear numberical stiuations; formulas, informal and formal solutions of simple linear equations |
| Intermediate Algebra | 25) | Other Equations \& Inequalities - representing other numberical situations; informal and formal solutions for inequalities \& more complex equations; use of alqebraic expressions \& inequalities |
|  | Data | Representation, Probability, \& Analysis |
| Data \& | 26) | Representing \& Interpreting Data - tables, charts, graphs; mean, median, mode, \& sampling |
| Statistics | 27) | Probability \& Uncertainty - concepts of "more likely" \& "less likely"; contingency tables, confidence intervals, hypothesis testing |

# Displays 14-16: Middle School Mathematics Areas Key 



## Glossary of Terms

$p$ value: The percent correct for an item across all subjects in the sample.
Standard Error (Mean): The standard error of the mean indicates how much the mean of a sample may differ from the true mean for the population. In general, the larger the sample drawn from a population, the smaller the standard error.

Mean: The mean is the sum of all scores divided by the total number of scores.
Median: The median is the middle of a distribution. One half of the scores lie below the median and one half lie above.

Interquartile Range: The Interquartile range is a measure of spread or dispersion. It is the range of scores from the $25^{\text {th }}$ to the $75^{\text {th }}$ percentiles.

Percentile: A percentile is a value below which lie $p \%$ of the values in the sample.
$25^{\text {th }}$ Percentile: The value where below this point lies the lowest $\frac{1}{4}$ ( $25 \%$ ) of scores.
$75^{\text {th }}$ Percentile: The value where above this point lies the highest $\frac{1}{4}$ ( $25 \%$ ) of scores.
Box and Whisker Plots: A box plot provides a visual summary of many important aspects of a distribution. The box stretches from the $25^{\text {th }}$ Percentile to the $75^{\text {th }}$ percentile, thus containing the middle half of the scores in the distribution. The Median, or $50^{\text {th }}$ percentile, is shown as a line across the box. The whiskers stretch from the $25^{\text {th }}$ and $75^{\text {th }}$ percentiles to the $5^{\text {th }}$ or the $95^{\text {th }}$ percentiles, respectively. [Note: Other criteria are sometimes used to define the "whiskers".]


Distribution of Scores: A visual or numerical description of the ranking of scores from lowest to highest often incorporating the relative frequencies of occurrence of each score.

Sample: A sample is a subset of a population.


[^0]:    Significantly Higher than the U.S.
    Not Significantly Different from U.S.
    Significantly Lower than the U.S.

[^1]:    Significantly Higher than the U.S.
    Not Significantly Different from U.S.
    Significantly Lower than the U.S.

